

# Estudo da resistência do ar

## Monitores:

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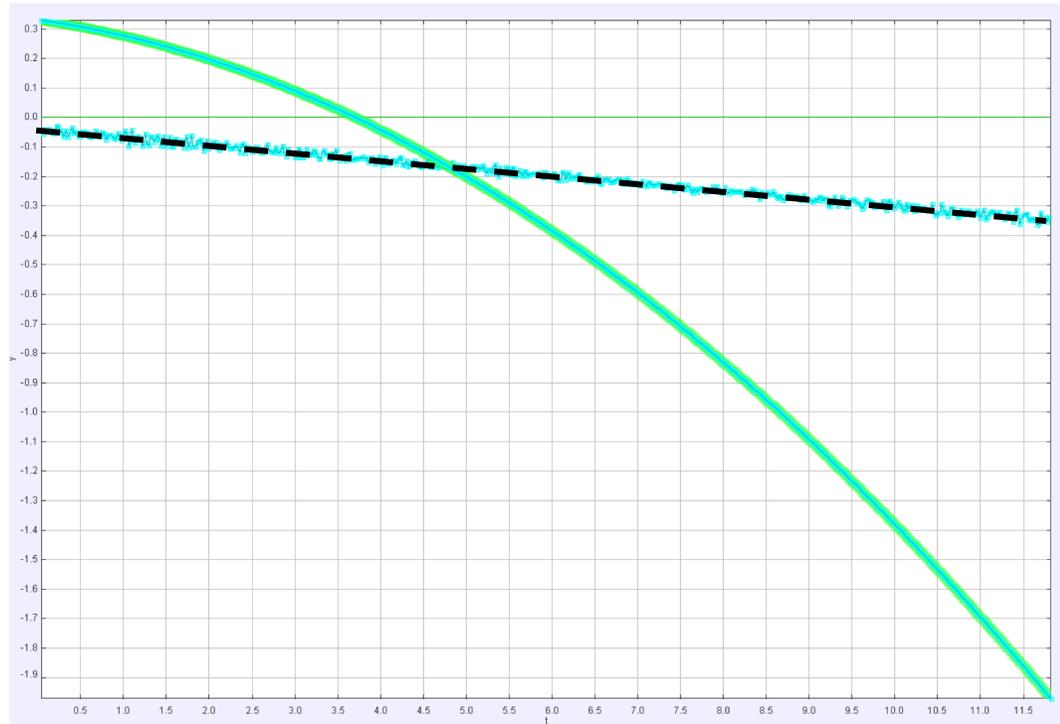
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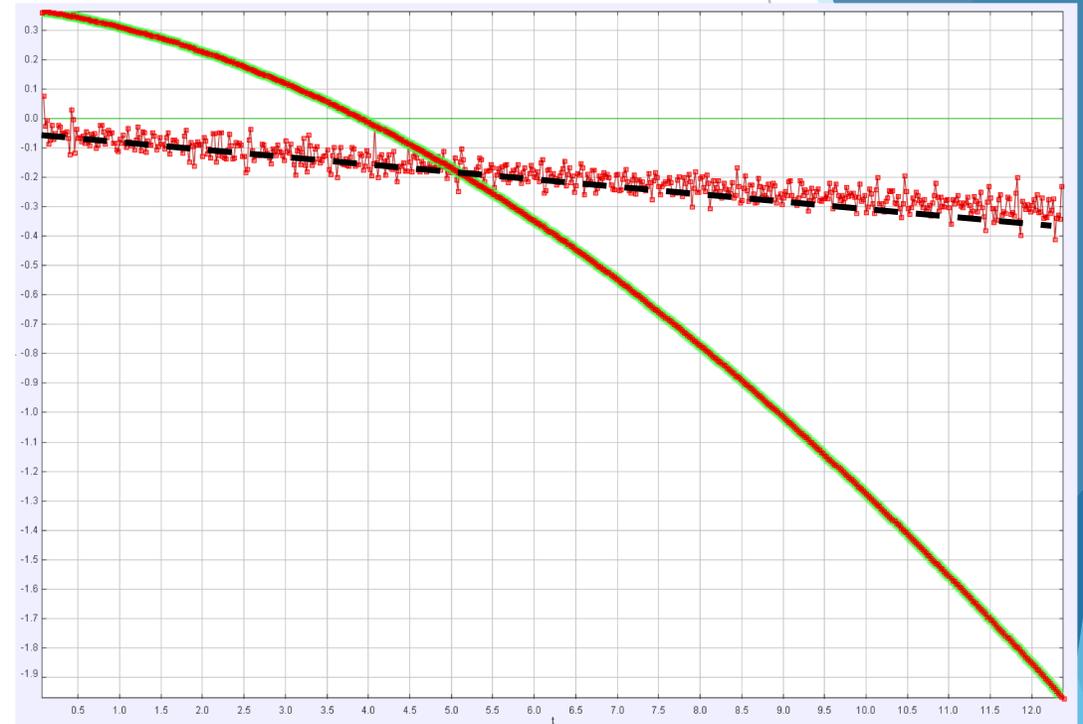
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Hipótese:  $F \propto v$   
 $F = -\gamma v$



Bola de metal



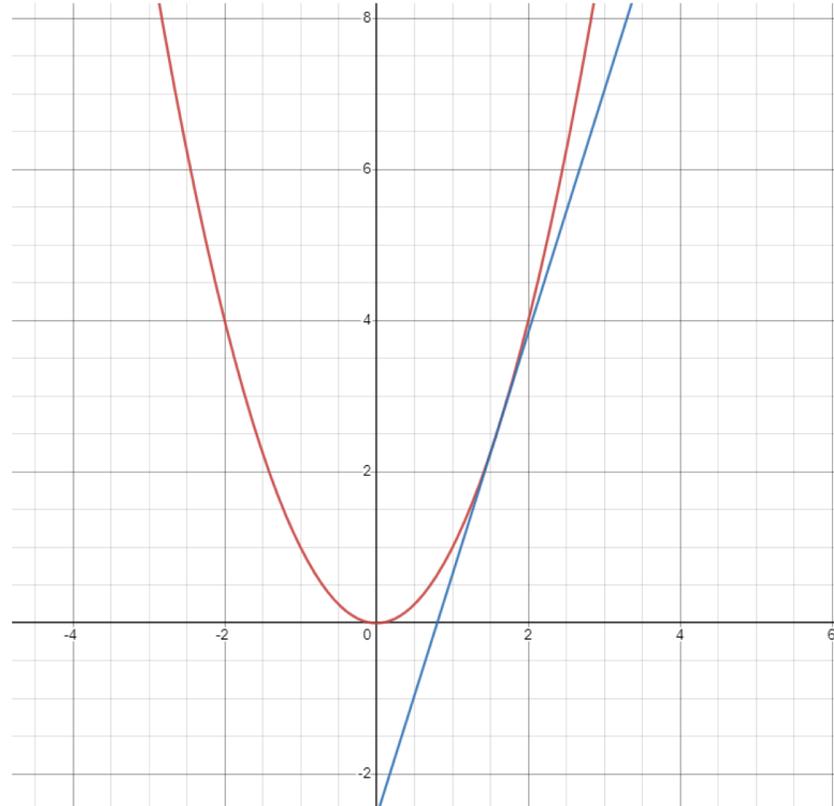
Bola de ping-pong

# Derivadas

▶  $\frac{dx}{dt} = \lim_{\Delta t \rightarrow 0} \frac{x(t+\Delta t) - x(t)}{\Delta t}$

▶  $v = \frac{dx}{dt}$

▶  $a = \frac{dv}{dt}$



# Equações do movimento

- ▶  $F = ma = m \frac{dv}{dt}$
- ▶ Sistema de equações:
  - ▶  $\frac{dv}{dt} = -g - \frac{\gamma}{m}v$
  - ▶  $v = \frac{dx}{dt}$

# Método de Euler

- ▶  $v = \frac{x(t+\Delta t)-x(t)}{\Delta t} \Leftrightarrow x(t + \Delta t) = v\Delta t + x(t)$
- ▶  $a = \frac{v(t+\Delta t)-v(t)}{\Delta t} \Leftrightarrow v(t + \Delta t) = a\Delta t + v(t)$
- ▶  $x[i] = v[i - 1]\Delta t + x[i - 1]$
- ▶  $v[i] = a[i - 1]\Delta t + v[i - 1]$

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x0=0
v0= 0
g = 10
b = 2.0
m=6
t0=0
tf=2.
dt=0.0001

N=int((tf-t0)/dt)

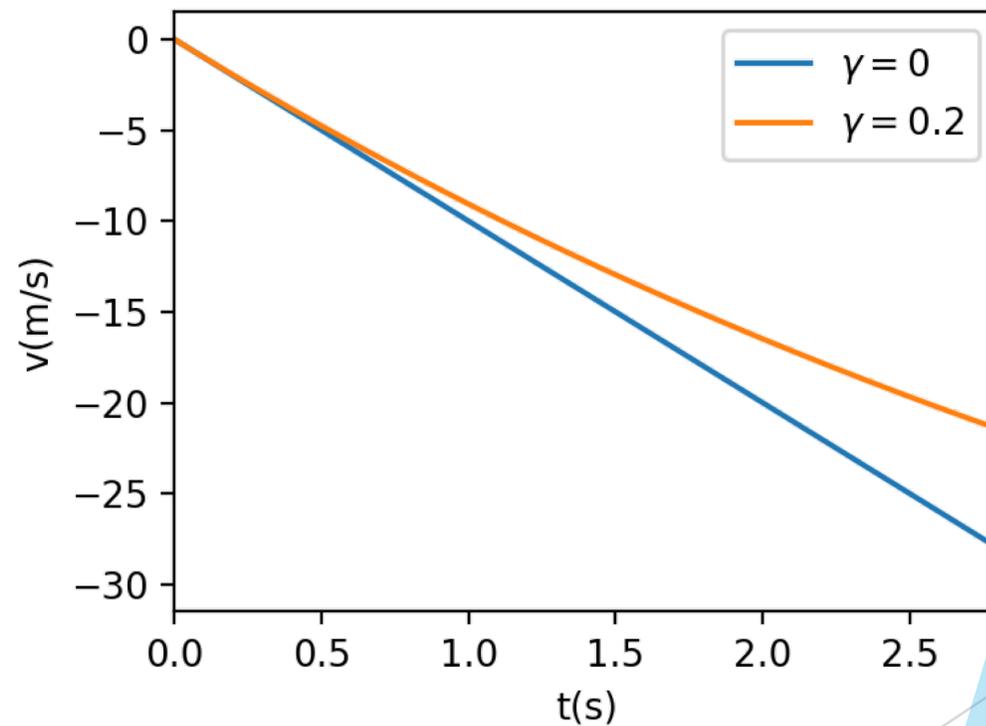
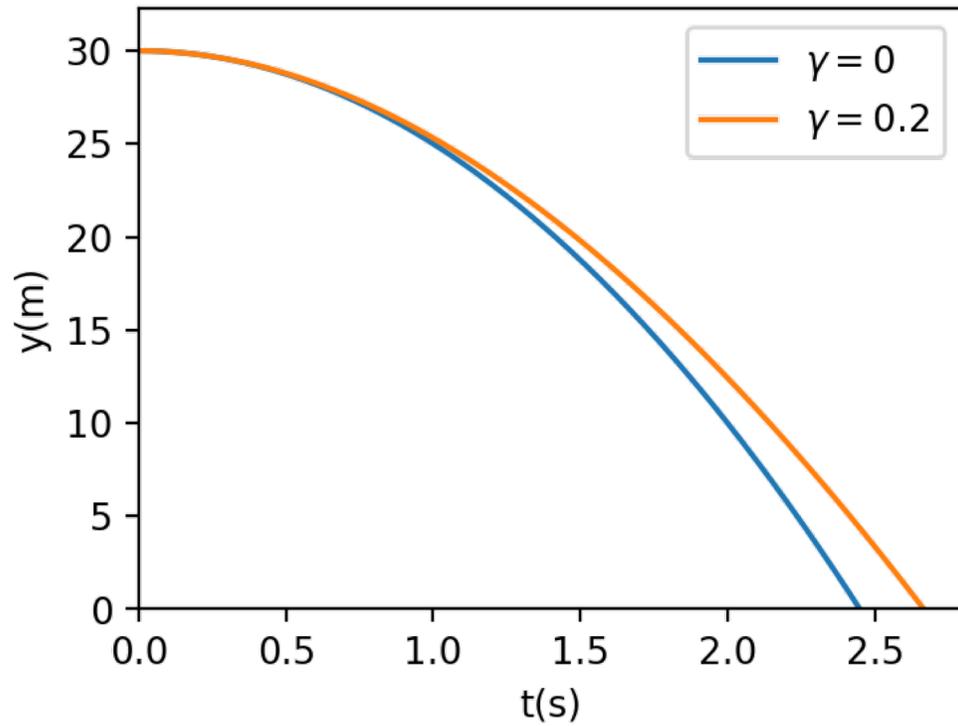
x= np.zeros(N)
x[0]= x0

v = np.zeros(N)
v[0]= v0

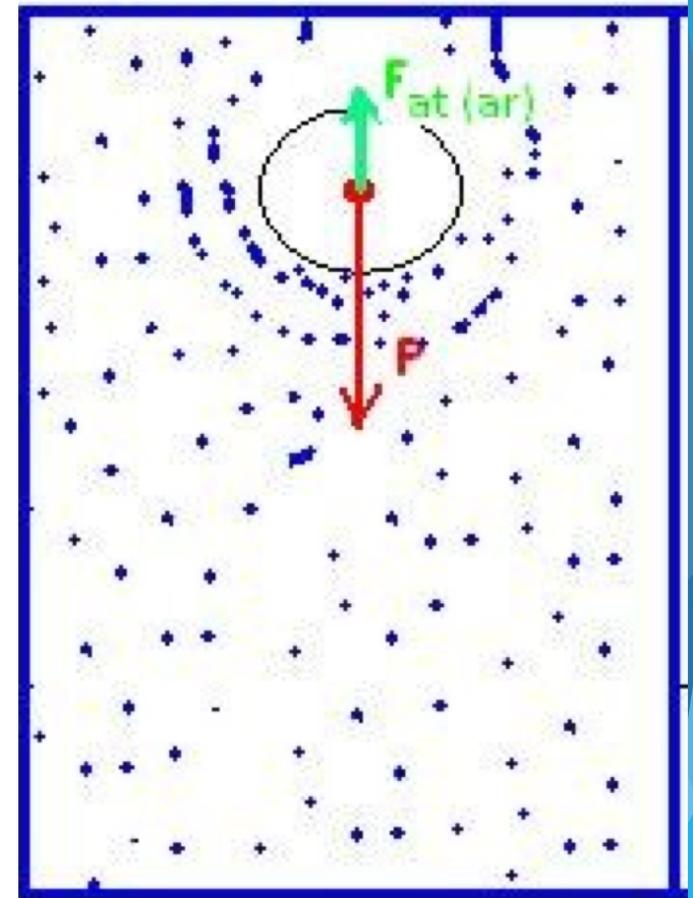
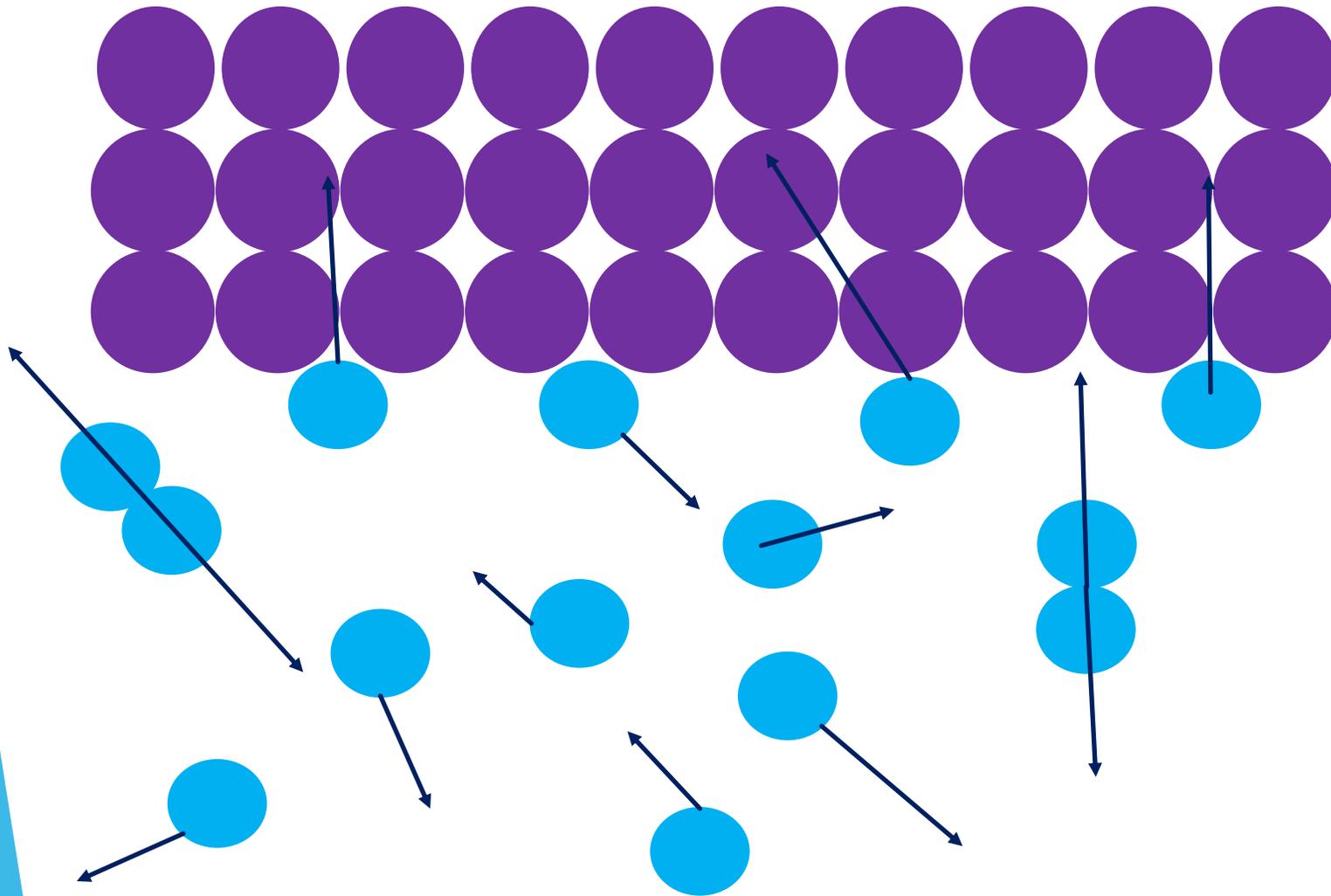
t=np.zeros(N)
t[0]= t0

for i in range(1,N):
    x[i]= x[i-1] + v[i-1]*dt
    v[i]= v[i-1] + (-g-b*v[i-1])*dt
    t[i]= t0 + dt*i
```

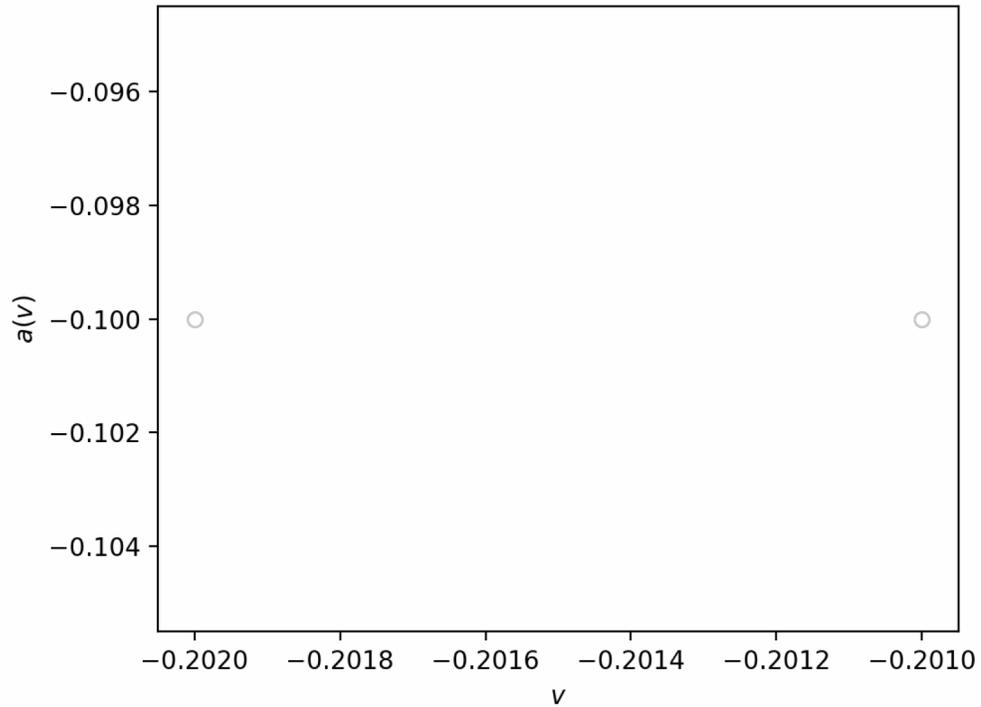
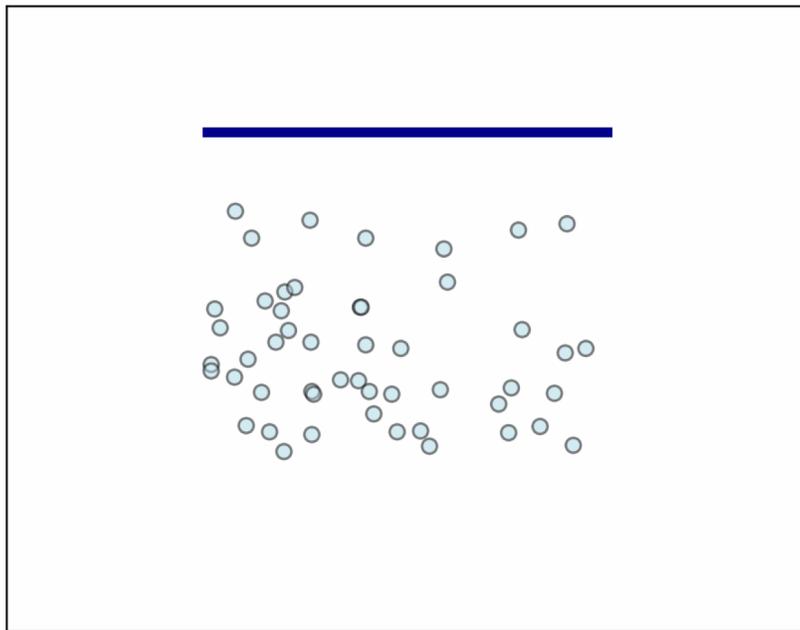
# Método de Euler



# O atrito a nível microscópico



# O atrito a nível microscópico



# Conclusões

- ▶ A força de atrito é dependente da velocidade
- ▶ Existem problemas na física que podem ser resolvidos utilizando simulações
- ▶ A força de atrito pode ser explicada pelas colisões entre as partículas do ar e o objeto.