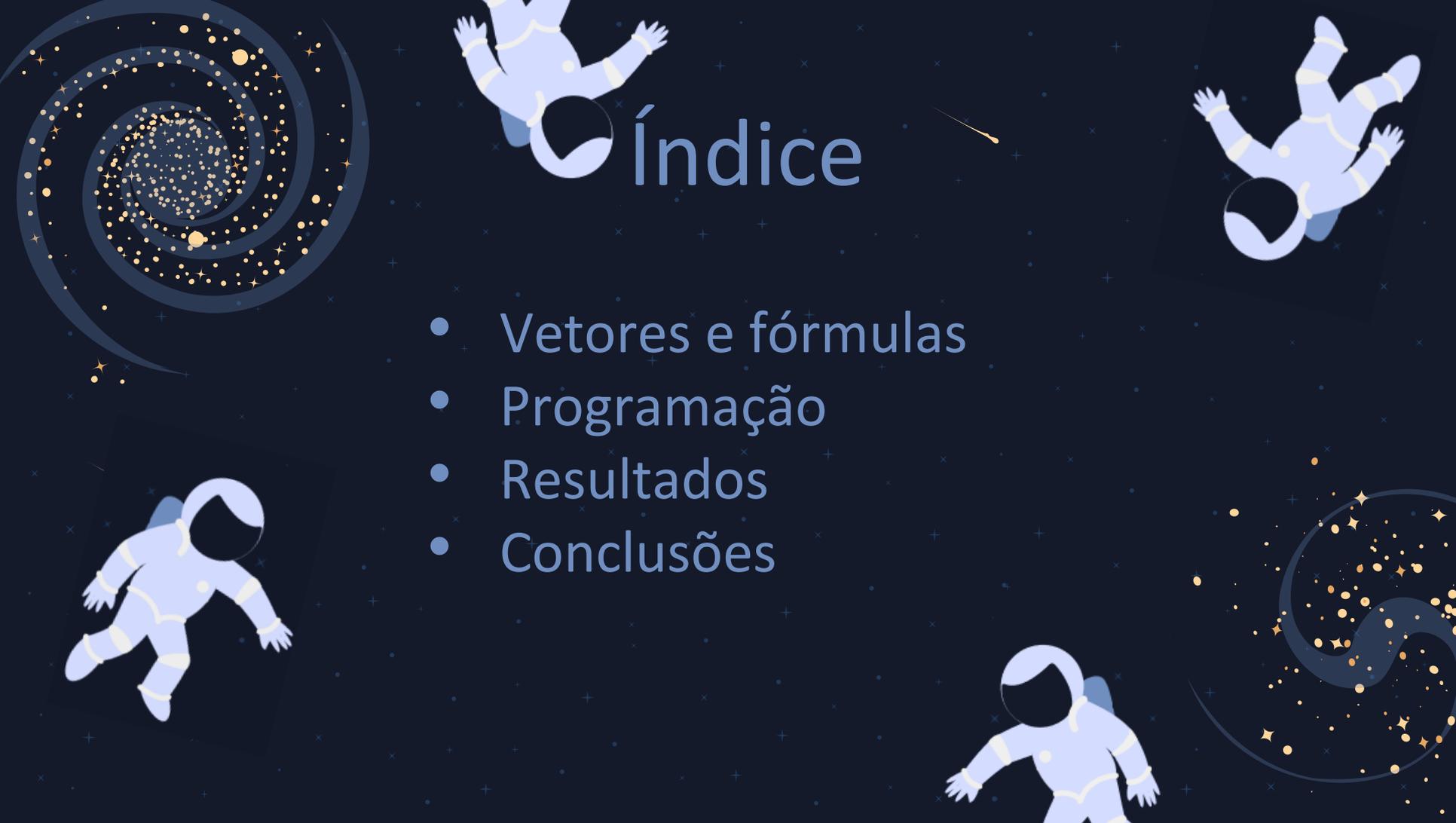


# Orbitas de uma sonda a volta de jupiter

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Projeto realizado por: Diogo  
David  
Maria  
Lourenço

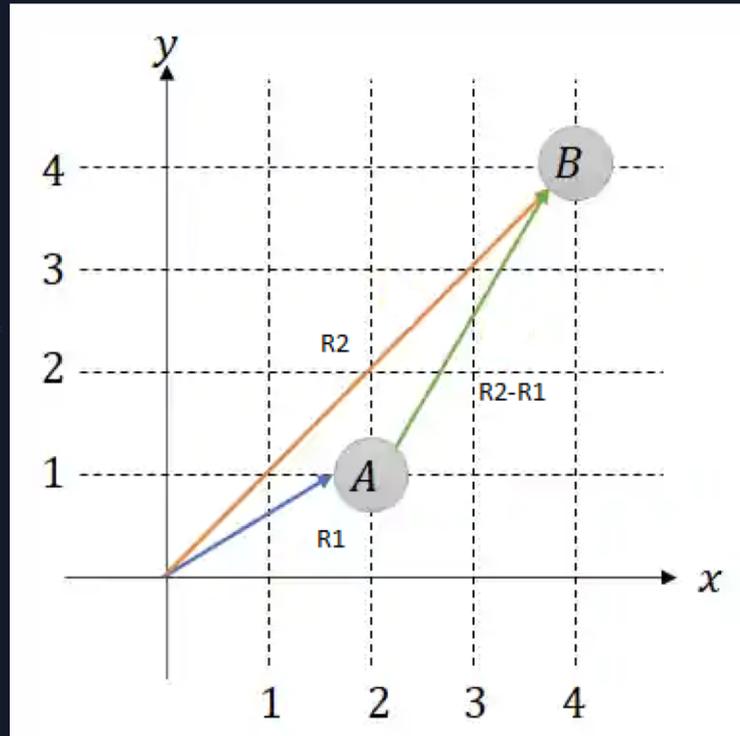




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- Vetores e fórmulas
- Programação
- Resultados
- Conclusões

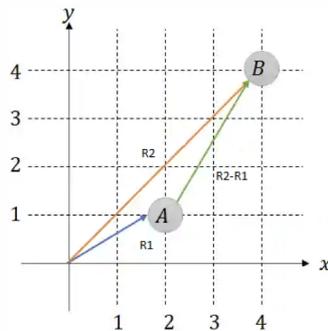
# Vetores de posição



# Força gravítica



$$Fg = G \times \frac{m.M}{r^2} \leftrightarrow \vec{Fg} = G \times \frac{m.M}{r^2} \times \hat{e}_{\vec{R2}-\vec{R1}} \leftrightarrow$$
$$\leftrightarrow \vec{Fg} = G \times \frac{m.M}{\|\vec{R2} - \vec{R1}\|^2} \times \frac{(\vec{R2} - \vec{R1})}{\|\vec{R2} - \vec{R1}\|} \leftrightarrow \vec{Fg} = G \times \frac{m.M \cdot (\vec{R2} - \vec{R1})}{\|\vec{R2} - \vec{R1}\|^3}$$



# Método de Euler

$$\left\{ \begin{array}{l} \frac{d\vec{R}}{dt} = \vec{v} \\ \frac{d\vec{v}}{dt} = \vec{a} = \frac{\vec{F}}{m} \end{array} \right. \Leftrightarrow \left\{ \begin{array}{l} \vec{v} = \frac{\vec{R}(\Delta t + t) - \vec{R}(t)}{\Delta t} \\ \frac{\vec{F}}{m} = \frac{\vec{v}(\Delta t + t) - \vec{v}(t)}{\Delta t} \end{array} \right. \Leftrightarrow$$

$$\Leftrightarrow \left\{ \begin{array}{l} \vec{R}(t + \Delta t) = \vec{v}\Delta t + \vec{R}(t) \\ \vec{v}(t + \Delta t) = \frac{\vec{F}}{m}\Delta t + \vec{v}(t) \end{array} \right.$$





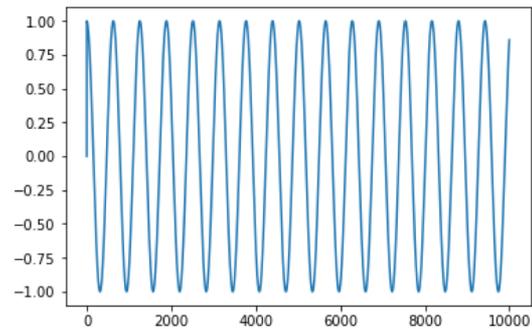
# Mola

```
In [31]: def time_step(x0,v0):  
         F=-1*x0  
         vf=v0+(F/1)*0.01  
         xf=x0+vf*0.01  
  
         return xf,vf
```

```
In [32]: x0,v0 = 1,0  
         for t in range (1,10001):  
             (xf,vf)=time_step(x0,v0)  
             (x0,v0)=(xf,vf)  
             X[t]=x0  
             print(xf,vf)
```

```
In [33]: plt.plot(X)
```

```
Out[33]: [<matplotlib.lines.Line2D at 0x15fe9f0>]
```



# Python



```
In [22]: def pitágoras(a,b):  
         c=((a**2)+(b**2))**0.5  
         return c
```

```
In [23]: pitágoras(1,1)
```

```
Out[23]: 1.4142135623730951
```

```
In [26]: pitagoras(3,4)
```

```
Out[26]: 5.0
```

```
In [ ]: def f_grav(x0,y0,m,M):  
        G=1 #6.67*10**-11  
        norma=((x0**2)+(y0**2))**0.5  
        R1=np.array([x0,y0])  
        Fg=(G*m*M*(-R1))/((norma)**3)  
        return Fg
```

```
In [54]: f_grav(0,2,1,1)
```

```
Out[54]: array([-0. ,  0.25])
```

$$\vec{R}_2(t) = (R \times \cos(wt), R \times \text{sen}(wt))$$

```
In [6]: def posjupiter(t,P,R):  
        w=(2*np.pi)/P  
        R2=np.array([R*np.cos(w*t),R*np.sin(w*t)])  
        return R2
```

```
In [20]: def f_grav(R1,m,M,R2):  
        G=6.67*10**-11  
        norma=((R1[0]-R2[0])**2)+((R1[1]-R2[1])**2)**0.5  
        Fg=(G*m*M*(R2-R1))/((norma)**3)  
        return Fg
```

```
In [5]: def time_step(r0,v0,m,M,R2):  
        rf=r0 + v0 * 360  
        F=f_grav(rf,m,M,R2)  
        vf=v0 + (F/m) * 360  
  
        return rf,vf
```

# Python



```
In [220]: P = 2*np.pi / 1.7134e-8
          R = 7.649 * 10**11
          R1 = np.array([7.592*10**11, 3.503*10**9])
          V0 = np.array([2510,10000])
          m = 1
          M = 1.9*10**27
```

```
In [222]: for i in range (0,50001):
          t=i*360
          R2=posjupiter (t,P,R)
          Rf,Vf=time_step(R1,V0,m,M,R2)
          Xs[i]=Rf[0]
          Ys[i]=Rf[1]
          Xj[i]=R2[0]
          Yj[i]=R2[1]
          V[i]=((Vf[0]**2)+(Vf[1]**2))**0.5
          Dist_jup[i] = np.sqrt((R1[0]-R2[0])**2+((R1[1]-R2[1])**2))
          R1=Rf
          V0=Vf
```

## Dados utilizados

Massa de Júpiter:  $1,9 \cdot 10^{27}$  Kg

Raio médio da órbita de Júpiter:  $7,649 \cdot 10^{11}$  m

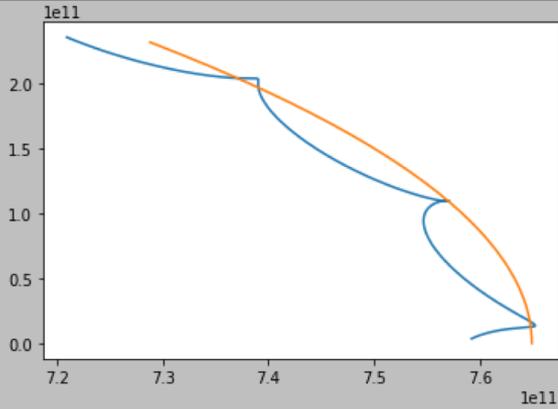
Período da órbita de Júpiter:  $3,67 \cdot 10^8$  s

Posição inicial de Júpiter:  $x=7,649 \cdot 10^{11}$  m,  $y=0$  m

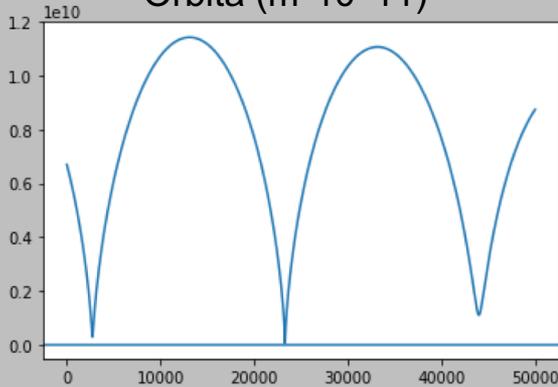
Posição inicial da sonda:  $x=7,592 \cdot 10^{11}$  m,  
 $y=3,503 \cdot 10^9$  m

Velocidade inicial da sonda: Variável

# Resultados

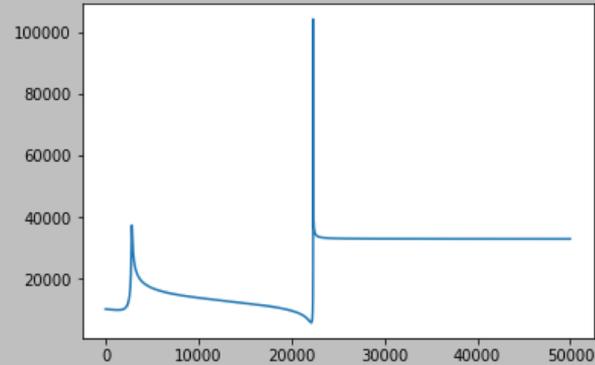


Órbita ( $m \cdot 10^{11}$ )



Distância a Júpiter ( $m \cdot 10^{10}$ )

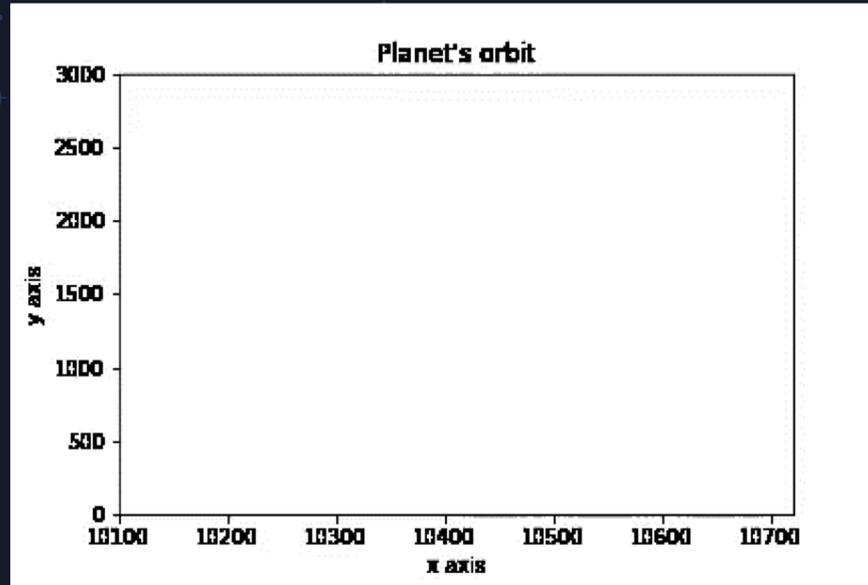
Velocidade inicial (m/s):  
( $V_x=2510; V_y=10000$ )  
Tempo de simulação: 5000 horas



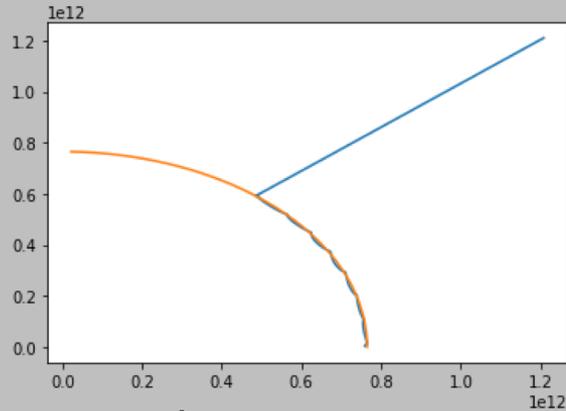
Velocidade (m/s)



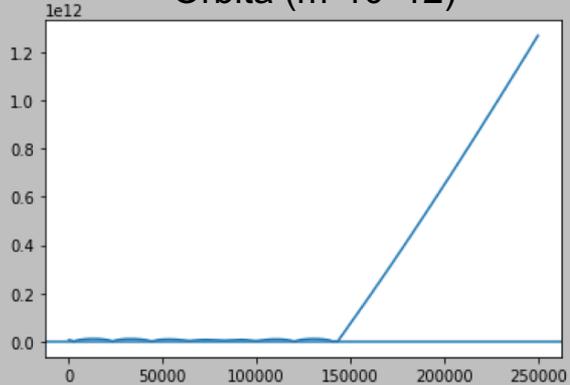
# Resultados



# Resultados

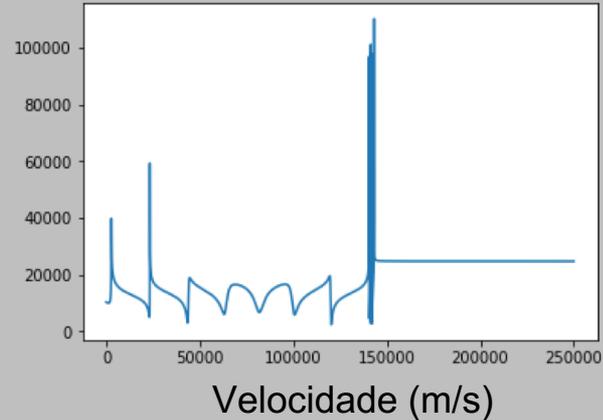


Órbita ( $m \cdot 10^{12}$ )

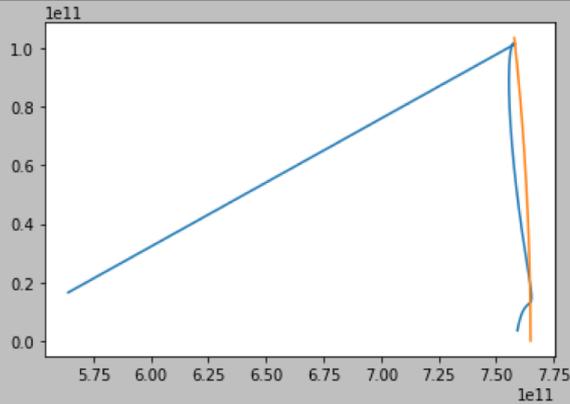


Distância a Júpiter ( $m \cdot 10^{12}$ )

Velocidade inicial (m/s):  
( $V_x=2510; V_y=10000$ )  
Tempo de simulação: 25000 horas

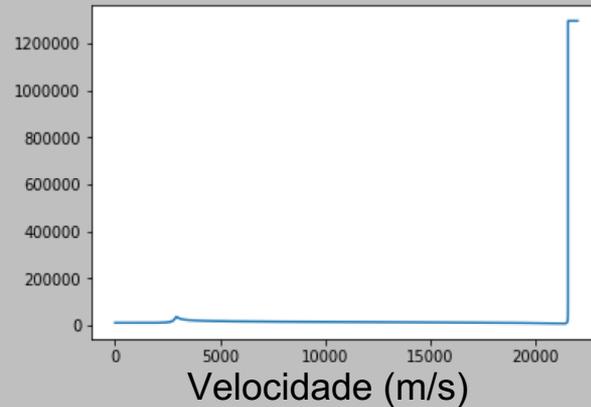
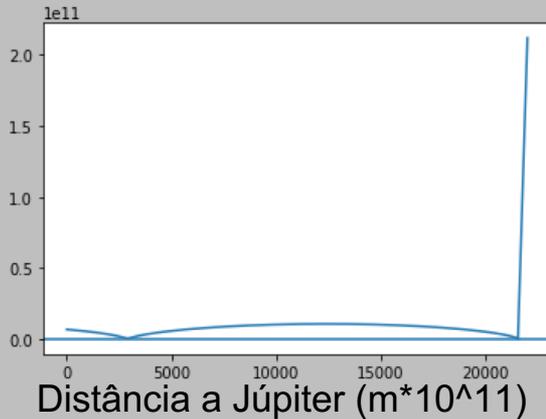


# Resultados

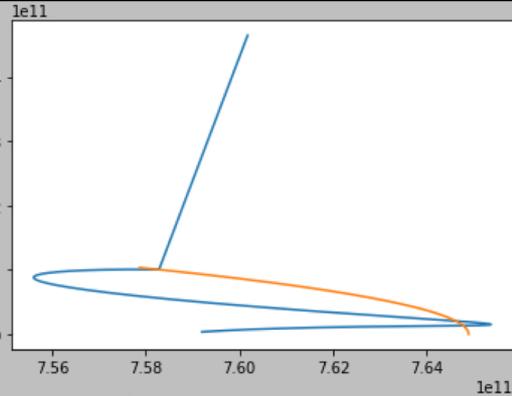


Órbita ( $m \cdot 10^{11}$ )

Velocidade inicial (m/s):  
( $V_x=2110$ ;  $V_y=10000$ )  
Tempo de simulação: 2200 horas

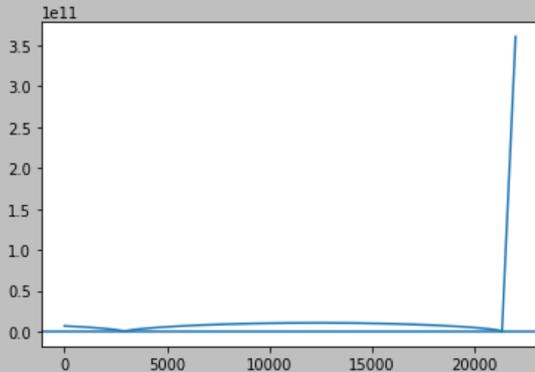


# Resultados

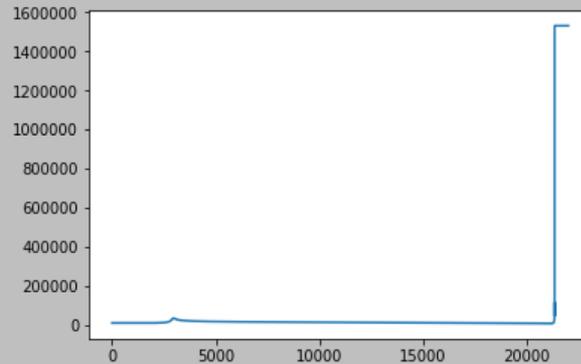


Órbita ( $m \cdot 10^{11}$ )

Velocidade inicial (m/s):  
( $V_x=2050$ ;  $V_y=10000$ )  
Tempo de simulação: 2200 horas

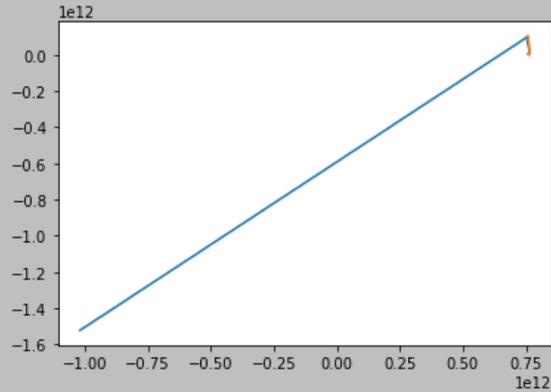


Distância a Júpiter ( $m \cdot 10^{11}$ )

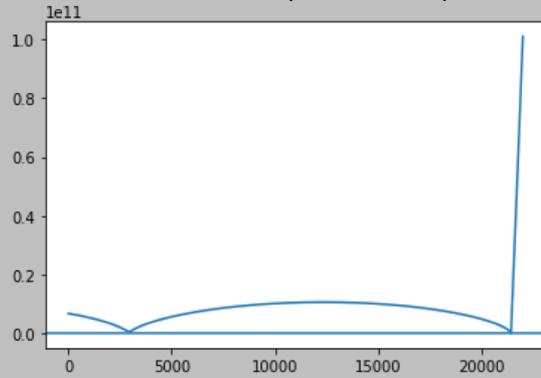


Velocidade (m/s)

# Resultados

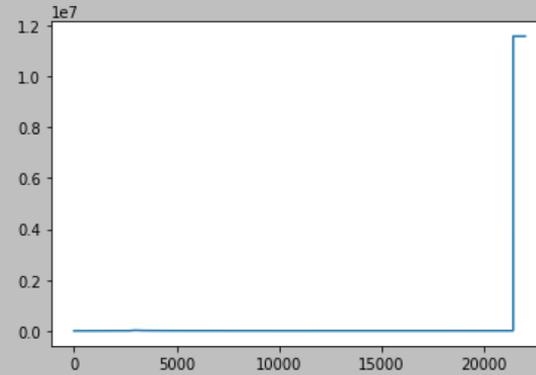


Órbita ( $m \cdot 10^{12}$ )



Distância a Júpiter ( $m \cdot 10^{11}$ )

Velocidade inicial (m/s):  
( $V_x=2050$ ;  $V_y=10000$ )  
Tempo de simulação: 2200 horas



Velocidade (m/s)

# Conclusões

