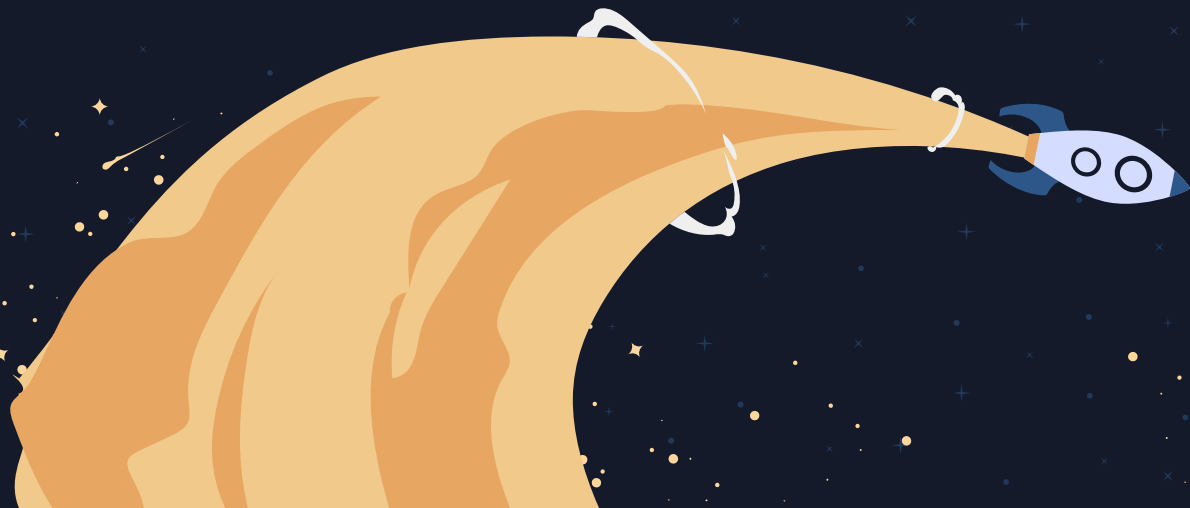


Orbitas de uma sonda a volta de jupiter

Projeto realizado por: Diogo
David
Maria
Lourenço

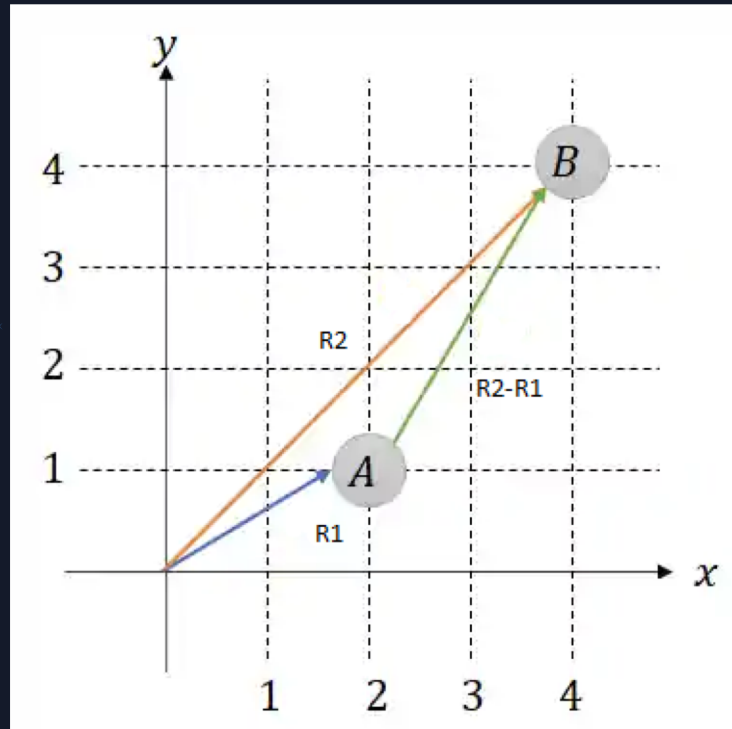




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- Vetores e fórmulas
- Programação
- Resultados
- Conclusões

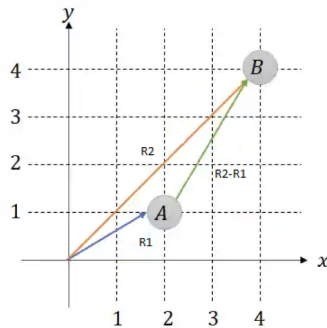
Vetores de posição



Força gravítica



$$Fg = G \times \frac{m.M}{r^2} \leftrightarrow \vec{Fg} = G \times \frac{m.M}{r^2} \times \hat{e}_{\vec{R2}-\vec{R1}} \leftrightarrow$$
$$\leftrightarrow \vec{Fg} = G \times \frac{m.M}{\|\vec{R2} - \vec{R1}\|^2} \times \frac{(\vec{R2} - \vec{R1})}{\|\vec{R2} - \vec{R1}\|} \leftrightarrow \vec{Fg} = G \times \frac{m.M \cdot (\vec{R2} - \vec{R1})}{\|\vec{R2} - \vec{R1}\|^3}$$



Método de Euler

$$\left\{ \begin{array}{l} \frac{d\vec{R}}{dt} = \vec{v} \\ \frac{d\vec{v}}{dt} = \vec{a} = \frac{\vec{F}}{m} \end{array} \right. \Leftrightarrow \left\{ \begin{array}{l} \vec{v} = \frac{\vec{R}(\Delta t + t) - \vec{R}(t)}{\Delta t} \\ \frac{\vec{F}}{m} = \frac{\vec{v}(\Delta t + t) - \vec{v}(t)}{\Delta t} \end{array} \right. \Leftrightarrow$$

$$\Leftrightarrow \left\{ \begin{array}{l} \vec{R}(t + \Delta t) = \vec{v}\Delta t + \vec{R}(t) \\ \vec{v}(t + \Delta t) = \frac{\vec{F}}{m}\Delta t + \vec{v}(t) \end{array} \right.$$





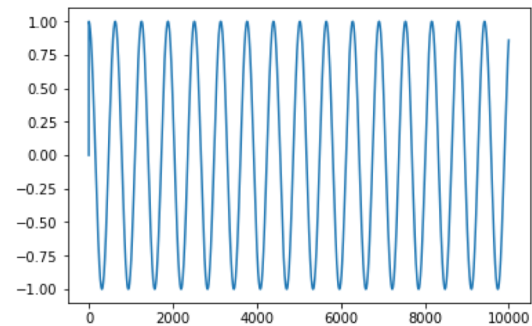
Mola

```
In [31]: def time_step(x0,v0):  
         F=-1*x0  
         vf=v0+(F/1)*0.01  
         xf=x0+vf*0.01  
  
         return xf,vf
```

```
In [32]: x0,v0 = 1,0  
         for t in range (1,10001):  
             (xf,vf)=time_step(x0,v0)  
             (x0,v0)=(xf,vf)  
             X[t]=x0  
             print(xf,vf)
```

```
In [33]: plt.plot(X)
```

```
Out[33]: [matplotlib.lines.Line2D at 0x15fe9f0]
```



Python



```
In [22]: def pitágoras(a,b):  
         c=((a**2)+(b**2))**0.5  
         return c
```

```
In [23]: pitágoras(1,1)
```

```
Out[23]: 1.4142135623730951
```

```
In [26]: pitagoras(3,4)
```

```
Out[26]: 5.0
```

```
In [ ]: def f_grav(x0,y0,m,M):  
        G=1 #6.67*10**-11  
        norma=((x0**2)+(y0**2))**0.5  
        R1=np.array([x0,y0])  
        Fg=(G*m*M*(-R1))/((norma)**3)  
        return Fg
```

```
In [54]: f_grav(0,2,1,1)
```

```
Out[54]: array([-0. ,  0.25])
```

$$\vec{R}_2(t) = (R \times \cos(wt), R \times \text{sen}(wt))$$

```
In [6]: def posjupiter(t,P,R):  
        w=(2*np.pi)/P  
        R2=np.array([R*np.cos(w*t),R*np.sin(w*t)])  
        return R2
```

```
In [20]: def f_grav(R1,m,M,R2):  
        G=6.67*10**-11  
        norma=((R1[0]-R2[0])**2)+((R1[1]-R2[1])**2)**0.5  
        Fg=(G*m*M*(R2-R1))/((norma)**3)  
        return Fg
```

```
In [5]: def time_step(r0,v0,m,M,R2):  
        rf=r0 + v0 * 360  
        F=f_grav(rf,m,M,R2)  
        vf=v0 + (F/m) * 360  
  
        return rf,vf
```

Python



```
In [220]: P = 2*np.pi / 1.7134e-8
R = 7.649 * 10**11
R1 = np.array([7.592*10**11, 3.503*10**9])
V0 = np.array([2510,10000])
m = 1
M = 1.9*10**27
```

```
In [222]: for i in range (0,50001):
t=i*360
R2=posjupiter (t,P,R)
Rf,Vf=time_step(R1,V0,m,M,R2)
Xs[i]=Rf[0]
Ys[i]=Rf[1]
Xj[i]=R2[0]
Yj[i]=R2[1]
V[i]=((Vf[0]**2)+(Vf[1]**2))**0.5
Dist_jup[i] = np.sqrt((R1[0]-R2[0])**2+((R1[1]-R2[1])**2))
R1=Rf
V0=Vf
```


Dados utilizados

Massa de Júpiter: $1,9 \cdot 10^{27}$ Kg

Raio médio da órbita de Júpiter: $7,649 \cdot 10^{11}$ m

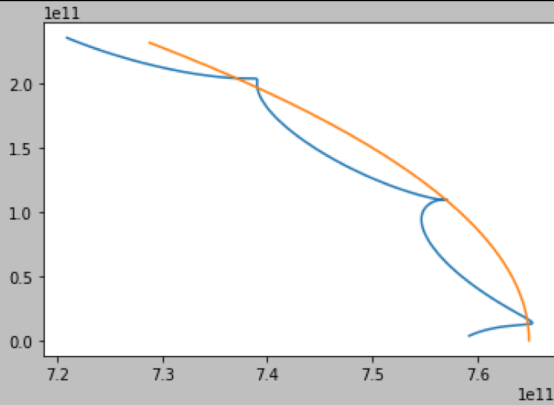
Período da órbita de Júpiter: $3,67 \cdot 10^8$ s

Posição inicial de Júpiter: $x=7,649 \cdot 10^{11}$ m, $y=0$ m

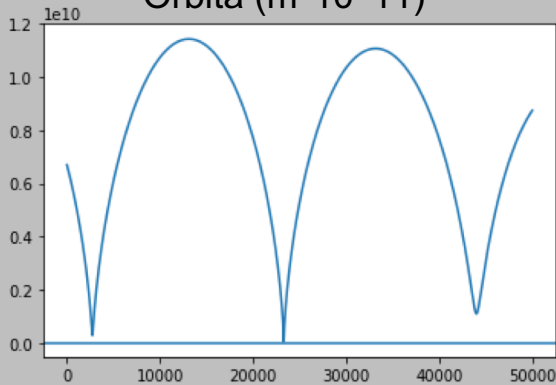
Posição inicial da sonda: $x=7,592 \cdot 10^{11}$ m,
 $y=3,503 \cdot 10^9$ m

Velocidade inicial da sonda: Variável

Resultados

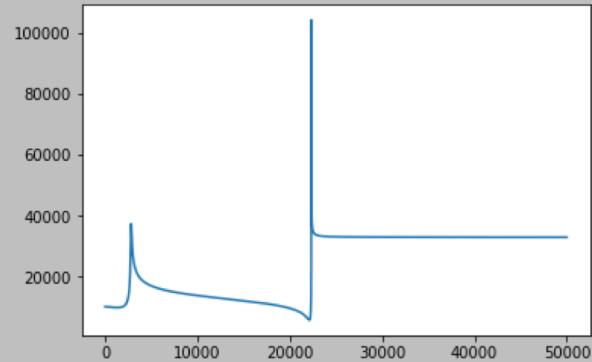


Órbita ($m \cdot 10^{11}$)



Distância a Júpiter ($m \cdot 10^{10}$)

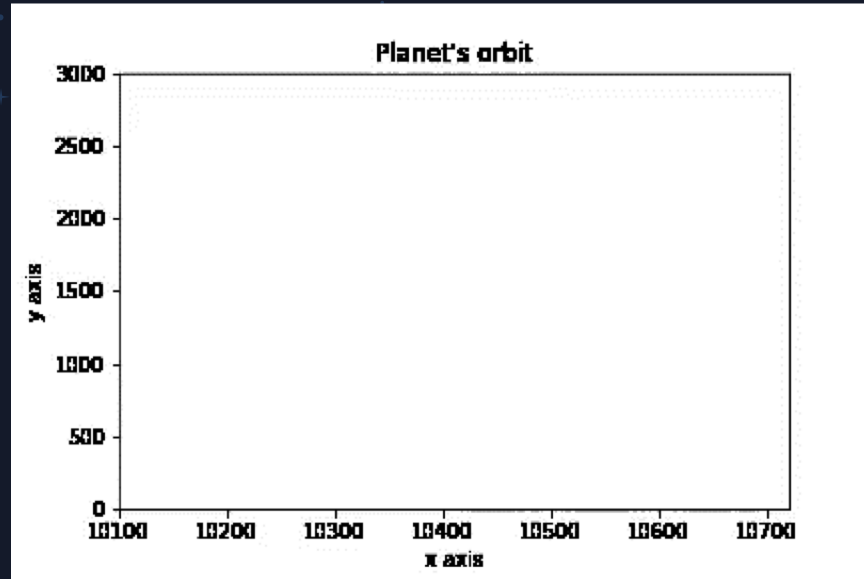
Velocidade inicial (m/s):
($V_x=2510; V_y=10000$)
Tempo de simulação: 5000 horas



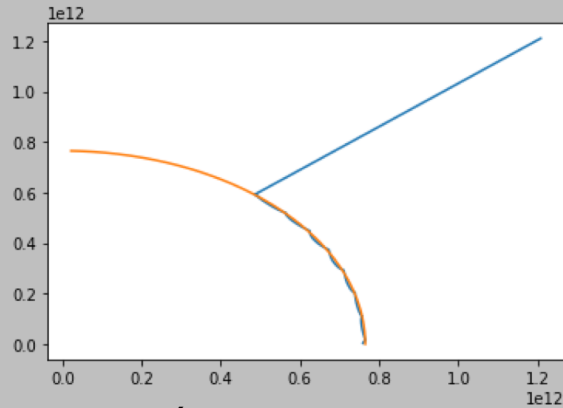
Velocidade (m/s)



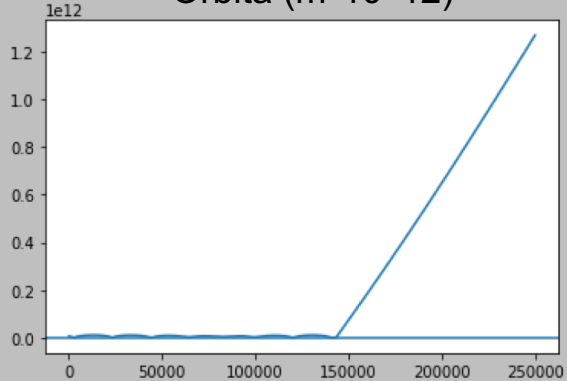
Resultados



Resultados

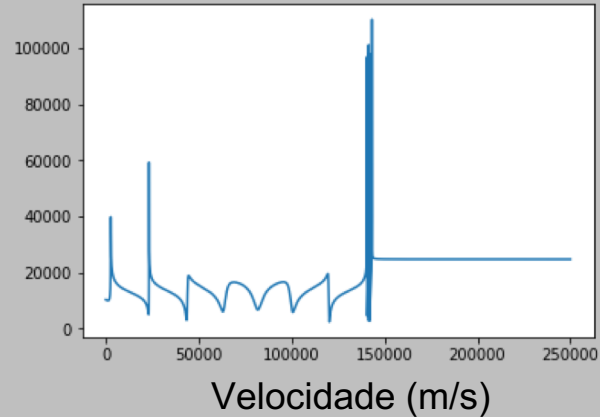


Órbita ($m \cdot 10^{12}$)

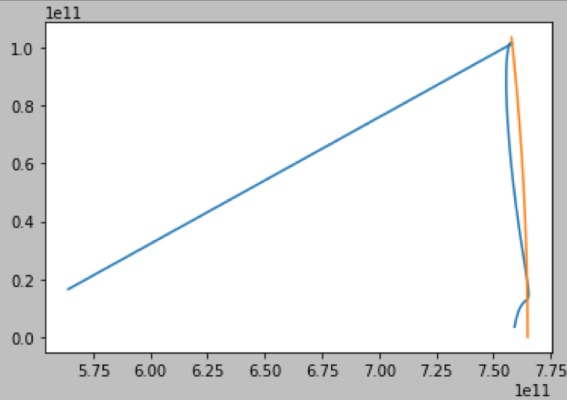


Distância a Júpiter ($m \cdot 10^{12}$)

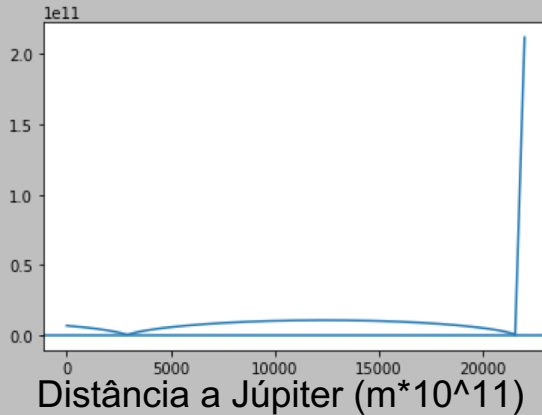
Velocidade inicial (m/s):
($V_x=2510$; $V_y=10000$)
Tempo de simulação: 25000 horas



Resultados

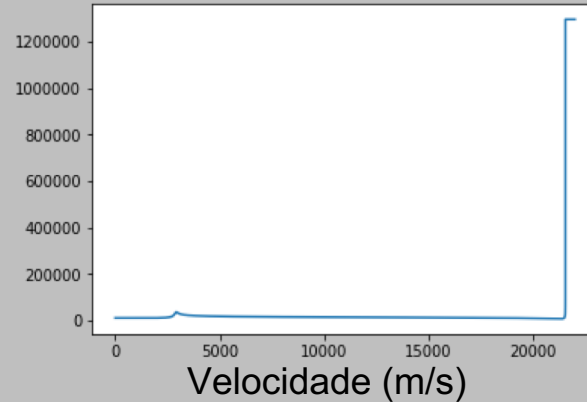


Órbita ($m \cdot 10^{11}$)

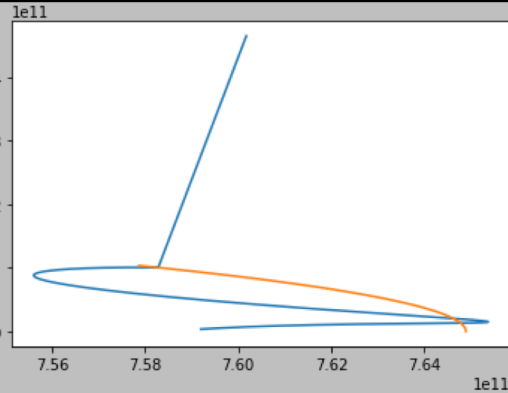


Distância a Júpiter ($m \cdot 10^{11}$)

Velocidade inicial (m/s):
($V_x=2110$; $V_y=10000$)
Tempo de simulação: 2200 horas

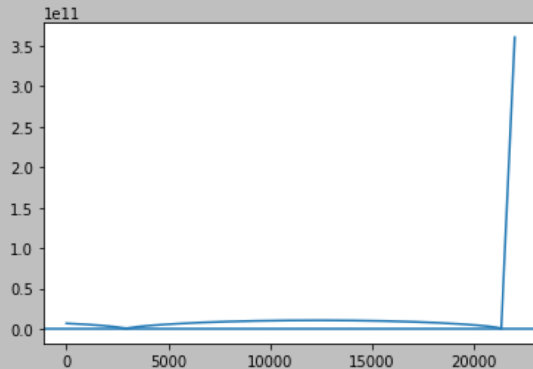


Resultados

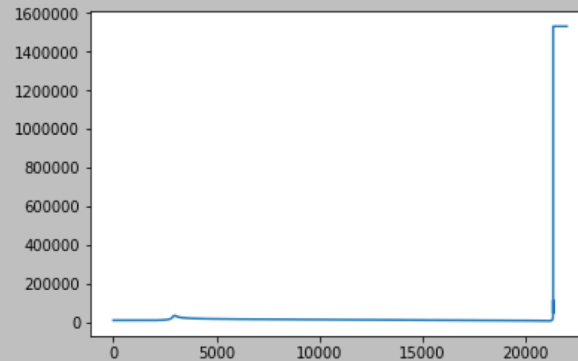


Órbita ($m \cdot 10^{11}$)

Velocidade inicial (m/s):
($V_x=2050$; $V_y=10000$)
Tempo de simulação: 2200 horas

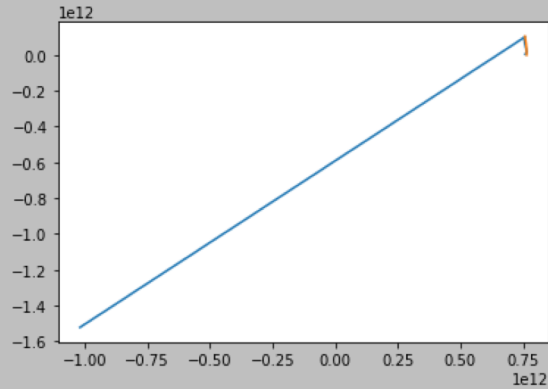


Distância a Júpiter ($m \cdot 10^{11}$)

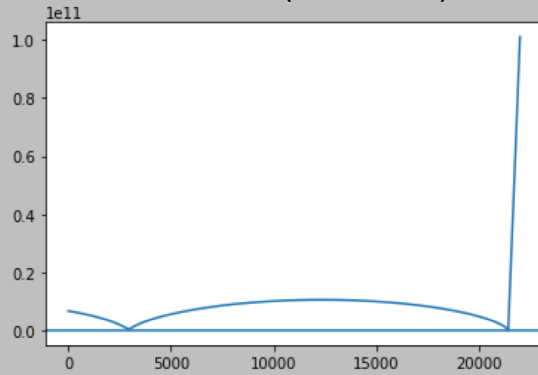


Velocidade (m/s)

Resultados

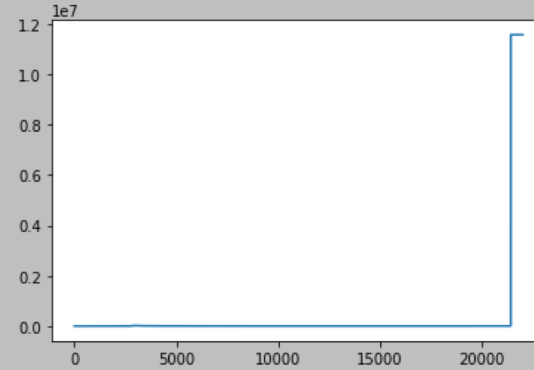


Órbita ($m \cdot 10^{12}$)



Distância a Júpiter ($m \cdot 10^{11}$)

Velocidade inicial (m/s):
($V_x=2050$; $V_y=10000$)
Tempo de simulação: 2200 horas



Velocidade (m/s)

Conclusões

